

Quantization of Continuous Data for Pattern Based Rule Extraction

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INTRODUCTION

A great deal of interesting real-world data is encountered through the analysis of continuous variables, however many of the robust tools for rule discovery and data characterization depend upon the underlying data existing in an ordinal, enumerable or discrete data domain. Tools that fall into this category include much of the current work in fuzzy logic and rough sets, as well as all forms of event-based pattern discovery tools based on probabilistic inference.

Through the application of discretization techniques, continuous data is made accessible to the analysis provided by the strong tools of discrete-valued data mining. The most common approach for discretization is quantization, in which the range of observed continuous valued data are assigned to a fixed number of quanta, each of which covers a particular portion of the range within the bounds provided by the most extreme points observed within the continuous domain. This chapter explores the effects such quantization may have, and the techniques that are available to ameliorate the negative effects of these efforts, notably fuzzy systems and rough sets.

BACKGROUND

Real-world data sets are only infrequently composed of discrete data, and any reasonable knowledge discovery approach must take into account the fact that the underlying data will be based on continuous-valued or mixed mode data. If one examines the data at the UCI Machine-Learning Repository (Newman, Hettich, Blake & Merz, 1998) one will see that many of the data sets within this group are continuous-valued; the majority of the remainder are based on measurements

of continuous valued random variables that have been pre-quantized before being placed in the database.

The tools of the data mining community may be considered to fall into the following three groups:

- minimum-error-fit and other gradient descent models, such as: support vector machines (Cristianini & Shawe-Taylor, 2000; Duda, Hart & Stork, 2001; Camps-Valls, Martínez-Ramón, Rojo-Álvarez & Soria-Olivas, 2004); neural networks (Rumelhart, Hinton & Williams, 1986); and other kernel or radial-basis networks (Duda, Hart & Stork, 2001; Pham, 2006)
- Bayesian-based learning tools (Duda, Hart & Stork, 2001), including related random-variable methods such as Parzen window estimation
- statistically based pattern and knowledge discovery algorithms based on an event-based model. Into this category falls much of the work in rough sets (Grzymala-Busse, & Ziarko, 1999; Pawlak, 1982, 1992; Singh & Minz, 2007; Slezak & Wroblewski, 2006), fuzzy knowledge representation (Boyen & Wehenkel, 1999; Gabrys 2004; Hathaway & Bezdek 2002; Höppner, Klawonn, Kruse & Runkler, 1999), as well as true statistical methods such as “pattern discovery” (Wang & Wong, 2003; Wong & Wang, 2003; Hamilton-Wright & Stashuk, 2005, 2006).

The methods in the last category are most affected by quantization and as such will be specifically discussed in this chapter. These algorithms function by constructing rules based on the observed association of data values among different quanta. The occurrence of a feature value within particular quanta may be considered an “event” and thereby all of the tools of information theory may be brought to bear. Without

the aggregation of data into quanta, it is not possible to generate an accurate count of event occurrence or estimate of inter-event relationships.

MAIN FOCUS

The discretization of continuous-valued data can be seen as a clustering technique in which the ranges of observed values are assigned to a limited set of Q cluster labels (sometimes referred to as a Borel set). The success or failure of a quantization structure may therefore be evaluated in terms of how well each of the Q clusters represents a homogenous and useful grouping of the underlying data.

The action of quantization is performed as a first step towards the discovery of the data topology, and therefore must frequently be undertaken without a great deal of knowledge of the underlying structure of the data. For this reason, such discretization is usually done using the information available in a single feature. Two major strategies for this are feature value *partitioning* and *quantization*.

Feature Value Partitioning

Partitioning schemes, such as those described in ID3 and C4.5 (Quinlan, 1986; 1993) as well as those used in the WEKA project (Witten & Frank, 2000) rely upon an analysis of decisions to be made within a single feature to provide a classification specific means of dividing the observed data values between labels. Quinlan (1993) provides an excellent discussion of an information-theoretic based approach to the construction of per-feature partitioning schemes in the discussion of the C4.5 classifier. In any such partitioning scheme, the placement of the partition is chosen as a means to optimize a classification decision made based on a single feature.

Quinlan's (1993) discussion is particularly salient, as it is in such tree-based classifiers that this treatment is the most advantageous, because the primary feature of a partitioning mechanism is that each feature is treated independently. This supports classification algorithms that are based on a decision tree, but does not support the discovery of multi-feature, high-order events. Furthermore, note that a classifier label value must be known in advance in order to use this technique; all

data is therefore viewed in terms of its ability to provide support for some particular label value.

Feature Value Quantization

Quantization, on the other hand, refers to the construction of a set of range-based divisions of the input feature space, where each distinct quantization "bin" represents a projection of an input feature through an aggregation scheme, independent of label value. By constructing such a quantization independently of class label values, it is therefore possible to support the discovery of data patterns independent of any potential classification structure. Feature value quantization underlies most fuzzy systems (Pedrycz, 1995; Pal & Mitra, 1999) as well as discrete information theoretic based approaches such as the "pattern discovery" algorithm (Wang & Wong, 2003; Wong & Wang, 2003; Hamilton-Wright & Stashuk, 2006).

It is through the introduction of uncertainty-management techniques that the "cost of quantization" may be ameliorated. This cost is inherent in the structure of the quantization resulting from a particular technique.

Properties of Quantization

The main strength of quantization is that by reducing a continuous domain problem to a discrete one, the powerful tools of event-based reasoning may be brought to bear. By taking a problem from the continuous domain to a discrete one, the random variables underlying the model of the continuous domain may be represented by discrete state variables, thereby allowing the representation of the data domain as a series of events with possible correlation (for an example, see Ross, 1985).

As an added benefit, such quantization provides protection against measurement noise (as analysis will be insensitive to perturbation in measurement value) provided such perturbation does not change the bin assignment. This simplifies the overall problem, reducing computational complexity, which in turn allows the application of algorithms that locate and analyze high-order patterns (*i.e.*; significant correlations between a large number of input features) such as the "pattern discovery" algorithm just mentioned.

All problems arising from the use of quantization stem from the fact that no quantization scheme can

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