

Chapter 1

Scatter Search and Path Relinking: A Tutorial on the Linear Arrangement Problem

Rafael Martí

Universidad de Valencia, Spain

Juan-José Pantrigo

Universidad Rey Juan Carlos, Spain

Abraham Duarte

Universidad Rey Juan Carlos, Spain

Vicente Campos

Universidad de Valencia, Spain

Fred Glover

OptTek Systems, Inc., USA

ABSTRACT

Scatter search (SS) and path relinking (PR) are evolutionary methods that have been successfully applied to a wide range of hard optimization problems. The fundamental concepts and principles of the methods were first proposed in the 1970s and 1980s, and were based on formulations, dating back to the 1960s, for combining decision rules and problem constraints. The methods use strategies for search diversification and intensification that have proved effective in a variety of optimization problems and that have sometimes been embedded in other evolutionary methods to yield improved performance. This paper examines the scatter search and path relinking methodologies from both conceptual and practical points of view, and identifies certain connections between their strategies and those adopted more recently by particle swarm optimization. The authors describe key elements of the SS & PR approaches and apply them to a hard combinatorial optimization problem: the minimum linear arrangement problem, which has been used in applications of structural engineering, VLSI and software testing.

DOI: 10.4018/978-1-4666-2479-5.ch001

1. INTRODUCTION

Scatter search (SS) was first introduced in Glover (1977) as a heuristic approach for general integer programming problems. SS systematically generates and updates a set of reference points that includes good solutions obtained by prior problem-solving efforts together with solutions that are screened to add diversity to the reference set. Path relinking (PR) was subsequently proposed in Glover (1989) and Glover and Laguna (1993) as an analog making use of neighborhood spaces in place of Euclidean spaces. Interesting relationships exist between the SS/PR approaches and the more recent particle swarm optimization methodology introduced by Kennedy and Eberhart (1995).

The SS and PR template (Glover, 1997) has served as a foundation for most of the SS and PR implementations to date, underscoring processes to take advantage of the flexibility of the SS and PR methodologies. Through these processes, each of the basic components can be implemented in a variety of ways and degrees of sophistication, and hence can be adapted conveniently to a variety of different problem settings. Advanced options derive from the way that five pivotal elements of the methods are implemented. We can find a large number of papers on both the SS method and the PR method and their applications. Glover and Laguna (1997) provide overviews and a variety of references on these methods and the monographic book on Scatter Search (Laguna & Martí, 2003) together with the feature cluster of the European Journal of Operational Research (Martí, 2006), which includes 19 papers, provide the reader with the elements to design successful SS implementations. A recent survey of SS and PR methods appears in Resende et al. (2010).

The following principles summarize the foundations of the scatter search and path relinking methodologies as evolved from its origins:

- Useful information about the form (or location) of optimal solutions is typically

contained in a suitably diverse collection of elite solutions.

- When solutions are combined as a strategy for exploiting such information, it is important to provide mechanisms capable of constructing combinations that extrapolate beyond the regions spanned by the solutions considered.
- The manner of combining solutions may be viewed as forming paths between (and beyond) them (using Euclidean spaces in SS and neighborhood spaces in PR). Each path results in introducing attributes of one elite solution into another, by a process where the trajectory for a given solution is influenced by the guidance of other solutions.
- It is likewise important to incorporate heuristic processes to map combined solutions into new solutions. The purpose of these combination mechanisms is to incorporate both diversity and quality.
- Taking account of multiple solutions simultaneously, as a foundation for creating combinations, enhances the opportunity to exploit information contained in the union of elite solutions.

A connection between the SS & PR approaches and particle swarm optimization (PSO) arises through the SS & PR strategy of combining solutions in a manner that may be interpreted as generating trajectories of selected elite solutions by reference to directions determined by other elite solutions (called guiding solutions in path relinking). In contrast to PSO, the solutions guided by SS & PR are initially generated and subsequently updated after the combination process by the application of associated heuristic or metaheuristic processes. PSO methods characteristically guide the progress of solutions in different streams of search by reference to the personal best of each stream and the global best overall streams.

19 more pages are available in the full version of this document, which may be purchased using the "Add to Cart" button on the publisher's webpage:

www.igi-global.com/chapter/scatter-search-path-relinking/70638

Related Content

Traffic Congestion Management as a Learning Agent Coordination Problem

Kagan Tumer, Zachary T. Welch and Adrian Agogino (2009). *Multi-Agent Systems for Traffic and Transportation Engineering* (pp. 261-279).

www.irma-international.org/chapter/traffic-congestion-management-learning-agent/26942

A Multi-Agent Modeling Approach to Simulate Dynamic Activity-Travel Patterns

Qi Han, Theo Arentze, Harry Timmermans, Davy Janssens and Geert Wets (2009). *Multi-Agent Systems for Traffic and Transportation Engineering* (pp. 36-56).

www.irma-international.org/chapter/multi-agent-modeling-approach-simulate/26932

Simulating UAV Surveillance for Analyzing Impact of Commitments in Multi-Agent Systems

David C. Han and Suzanne K. Barber (2012). *International Journal of Agent Technologies and Systems* (pp. 1-16).

www.irma-international.org/article/simulating-uav-surveillance-analyzing-impact/66066

Virtual Enterprise as a Multi Agent System

George Wamamu Musumba and Patrick Kanyi Wamuyu (2016). *International Journal of Agent Technologies and Systems* (pp. 46-68).

www.irma-international.org/article/virtual-enterprise-as-a-multi-agent-system/193957

Initial Formulation of an Optimization Method Based on Stigmergic Construction

Aditya C. Velivelli and Kenneth M. Bryden (2011). *International Journal of Agent Technologies and Systems* (pp. 19-36).

www.irma-international.org/article/initial-formulation-optimization-method-based/60652