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# Weakness of Association Rules: A Mechanism for Clustering

Rajesh Natarajan, IT & Systems Group, Indian Institute of Management Lucknow, Lucknow - 226 013, Uttar Pradesh, India, T: +91-522-2736659, F: +91-522-2734025, rajeshn@iiml.ac.in

B. Shekar, Quantitative Methods & Information Systems Area, Indian Institute of Management Bangalore, Bangalore - 560 076, Karnataka, India, T: +91-80-26993093, F: +91-80-26584050, shek@iimb.ernet.in

#### ABSTRACT

We introduce the notion of *weakness* of an AR. After providing the intuition, we develop a *weakness-based* distance-function for clustering ARs. We cluster ARs obtained from a small artificial data set through the average-linkage method. The clusters are compared with those obtained by applying a commonly used method to the same data-set.

#### **1. INTRODUCTION**

Rule immensity is an important issue in Association Rule (AR) mining. This problem concerns the multitude of discovered rules that hinder easy comprehension. We define *Weakness* as the extent to which an AR is unable to explain the presence of its constituent items. Weakness is then used as a heuristic to group ARs. Rules with similar *weakness* are placed in the same cluster, thus facilitating easy exploration of connections among them. A user needs to examine only those rules in 'relevant' clusters.

Lent, Swami and Widom [6] introduced the notion of 'clustered' ARs. Adomavicius and Tuzhilin [1] adopted an expert-driven, attribute hierarchy-based similar rule-grouping approach. The distance measure proposed by Toivonen, et al. [8] and Gupta and others [3] clustered rules that 'cover' the same set of transactions. One limitation of [8,3] is the arbitrariness of distance measures [1].

Dong and Li [2] introduced a distance metric for detecting unexpected rules. Sahar's  $d_{sc}$  [7] utilized both syntactic matching of item-sets and rule coverage of data. Jorge [5] studied clustering in the context of thematic browsing and summarization of large sets of ARs. Current research has concentrated either on syntactic (item-matching based) comparison [1,2,5] or on transaction-set coverage [3,7,8]. These approaches do not utilize certain intrinsic properties of ARs. We propose *weakness* (an intrinsic property)-based identification of specificity/generality of the AR in describing the presence of its constituents in the database.

#### 2. WEAKNESS OF AN ASSOCIATION RULE

Consider an AR,  $R: a_1 a_2 ... a_m \rightarrow a_{m+1} a_{m+2} ... a_n$ , having support  $S_R$  and confidence  $C_R$ . If all items of R are present in that transaction (*t*), then R covers *t*. Let the support of an individual item  $a_i \in R$  with respect to database D be  $Sa_i$ . R accounts for only  $S_R$ % of transactions in the database and does

not explain the portion (of D) containing  $1 \frac{S_R}{S_{a_i}}$  % of transactions

containing  $a_i$ . This fraction may be viewed as *weakness* of R with respect

to its constituent 
$$a_i: w_{a_i} = 1 \frac{S_R}{S_{a_i}}$$
 (1)

Weakness of an AR with respect to all its constituents is given by:

$$w_{R} = \frac{1}{n} \sum_{a_{i}} 1 \frac{S_{R}}{S_{a_{i}}}; a_{i} = \{a_{1}, a_{2}, ..., a_{n}\}$$
(2)

'w-value' brings out the strength of relationship between an AR and its constituents. A low w-value indicates strong characterization of its constituent items, since most of the transactions containing R's constituent items exhibit the behaviour captured by R. In addition, a low w-value signifies generality (wider coverage in D) of the relationship described by R. In contrast, a high w-value indicates specificity of the relationships revealed by the rule.

#### **3.** A WEAKNESS-BASED DISTANCE MEASURE $(d_{m})$

Low generality of a high *w*-value rule suggests that relationships between the rule's items and items present in other rules may be worth exploring. Actions taken only on the basis of a high *w*-value (high-specificity) rule could be skewed as the rule brings out only one aspect of the items' behaviour in the database. Since *weakness* reflects the presence of relationships among constituents, action based on rules with equal or near-equal values could yield similar results.

We define weakness-based distance as:

$$d_{w}(R_{1}, R_{2}) \quad \frac{|w_{1} \quad w_{2}|}{w_{1} \quad w_{2}}, \ 0 \le w_{l}, w_{2} \le 1.$$
(3)

Any difference  $\Delta w$  results in a larger distance for low *w*-values and smaller distance for high *w*-values. If  $(|w_1 \cdot w_2| = |w_3 \cdot w_4|)$  and  $(w_1 + w_2 \le w_3 + w_4)$ , then  $d_w(R_1, R_2) > d_w(R_3, R_4)$ . Let  $w_1 = 0.4$ ,  $w_2 = 0.2$ ,  $w_3 = 0.8$  and  $w_4 = 0.6$ . Then,  $d_w(R_1, R_2) = 0.3333$  while  $d_w(R_3, R_4) = 0.14285$ . This may seem counter intuitive. However it has a rationale.  $R_1$  and  $R_2$  are unable to explain 40% and 20% respectively of their constituent items' presence. Thus, they are more general than  $R_3$  and  $R_4$  whose *w*-values are 0.8 and 0.6 respectively.  $R_3$  and  $R_4$  have poorer explanatory power than  $R_1$  and  $R_2$ , with respect to their constituent items.

This rationale has an analogical intuitive support. Consider four individuals  $A(R_i)$ ,  $B(R_2)$ ,  $C(R_3)$  and  $D(R_4)$ . Assume A and B possess deeper knowledge (of a topic) than C and D. Let the absolute difference in the knowledge-levels between the individuals in each of  $\{A,B\}$  and  $\{C,D\}$  be the same. Since A and B are quite knowledgeable, the difference would seem to be larger because it would require more effort to move from A's knowledge-level to B's knowledge-level. This greater effort may be due to the subtle and conceptually deeper knowledge required. However, it may be relatively easier to bridge the gap between C and D. Fewer facts and straightforward knowledge acquisition may suffice. Similarly,  $R_i$  and  $R_2$  may have good explanatory power and hence they may be separated by a larger distance than the more specific pair  $\{R_i, R_i\}$ .

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Table 1. An artificial transaction dataset

Transaction	Nos.	Transaction	Nos.
{Bread,Butter}	6	{Bread,Jam}	5
{Bread,Milk}	4	{Bread,Butter,Milk}	10
{Milk,Chocolate}	6	{Chocolate,Biscuit}	8
{Milk,Chocolate,Biscuit}	11	{Butter,Milk}	3
{Pen,Pencil,Eraser}	13	{Pencil,Eraser}	7
{Chocolate,Pencil,Eraser}	3	{Pen,Eraser}	3
{Chocolate,Biscuit,Pencil}	5	{Bread,Butter,Milk,Jam}	4
{Bread,Jam,Milk}	12		

Table 2. Association Rules extracted from transaction set of Table 1

No	Rule	Support	Confidence	Weakness
$\mathbf{R}_1$	Butter→Bread	0.20	0.86957	0.321315
<b>R</b> <sub>2</sub>	Jam→Bread	0.21	1.00	0.243902
R <sub>3</sub>	Bread→Milk	0.30	0.7317	0.334146
$R_4$	Butter→Milk	0.17	0.73913	0.460435
R <sub>5</sub>	Butter,Milk→Bread	0.14	0.82353	0.589947
R <sub>6</sub>	Chocolate→ Biscuit	0.24	0.72727	0.136364
$\mathbf{R}_7$	$Milk, Biscuit {\rightarrow} Chocolate$	0.11	1.00	0.662778
$R_8$	Pen→Pencil,Eraser	0.13	0.8125	0.407738
$\mathbf{R}_9$	Pen→Pencil	0.13	0.8125	0.361607
$R_{10}$	Pencil→Eraser	0.23	0.82143	0.146978
R <sub>11</sub>	Pen→Eraser	0.16	1.00	0.192308
$\mathbf{R}_{12}$	Jam,Milk $\rightarrow$ Bread	0.16	1.00	0.509284
$R_{13}$	Jam→Milk	0.16	0.76190	0.459048
$R_{14}$	$Chocolate {\rightarrow} Milk$	0.17	0.51515	0.572424

Table 3.  $d_{w}$  -based clustering

Step_No	Clusters	
1	{ <b>R</b> <sub>13</sub> , <b>R</b> <sub>4</sub> }	[0.002]
2	$\{\mathbf{R}_{14}, \mathbf{R}_5\}; \{\mathbf{R}_{13}, \mathbf{R}_4\}$	[0.015]
3	$\{\mathbf{R}_{3},\mathbf{R}_{1}\};\{\mathbf{R}_{14},\mathbf{R}_{5}\};\{\mathbf{R}_{13},\mathbf{R}_{4}\}$	[0.020]
4	$\{\mathbf{R}_{10}, \mathbf{R}_{6}\}; \{\mathbf{R}_{3}, \mathbf{R}_{1}\}; \{\mathbf{R}_{14}, \mathbf{R}_{5}\}; \{\mathbf{R}_{13}, \mathbf{R}_{4}\}$	[0.037]
5	$\{\mathbf{R}_{3}, \mathbf{R}_{1}, \mathbf{R}_{9}\}; \{\mathbf{R}_{10}, \mathbf{R}_{6}\}; \{\mathbf{R}_{14}, \mathbf{R}_{5}\}; \{\mathbf{R}_{13}, \mathbf{R}_{4}\}$	[0.049]
6	$\{\mathbf{R_{13}}, \mathbf{R_4}, \mathbf{R_{12}}\}; \{\mathbf{R_3}, \mathbf{R_1}, \mathbf{R_9}\}; \{\mathbf{R_{10}}, \mathbf{R_6}\}; \{\mathbf{R_{14}}, \mathbf{R_5}\}$	[0.051]
7	$\{\mathbf{R}_{14}, \mathbf{R}_5, \mathbf{R}_7\}; \{\mathbf{R}_{13}, \mathbf{R}_4, \mathbf{R}_{12}\}; \{\mathbf{R}_3, \mathbf{R}_1, \mathbf{R}_9\}; \{\mathbf{R}_{10}, \mathbf{R}_6\}$	[0.066]
8	$\{\mathbf{R}_{8}, \mathbf{R}_{13}, \mathbf{R}_{4}, \mathbf{R}_{12}\}; \{\mathbf{R}_{14}, \mathbf{R}_{5}, \mathbf{R}_{7}\}; \{\mathbf{R}_{3}, \mathbf{R}_{1}, \mathbf{R}_{9}\}; \{\mathbf{R}_{10}, \mathbf{R}_{6}\}$	[0.077]
9	$\{\mathbf{R_{11}}, \mathbf{R_2}\}; \{\mathbf{R_8}, \mathbf{R_{13}}, \mathbf{R_4}, \mathbf{R_{12}}\}; \{\mathbf{R_{14}}, \mathbf{R_5}, \mathbf{R_7}\}; \{\mathbf{R_3}, \mathbf{R_1}, \mathbf{R_9}\}; \{\mathbf{R_{10}}, \mathbf{R_6}\}$	[0.118]
10	$\{\mathbf{R}_{8}, \mathbf{R}_{13}, \mathbf{R}_{4}, \mathbf{R}_{12}, \mathbf{R}_{14}, \mathbf{R}_{5}, \mathbf{R}_{7}\}; \{\mathbf{R}_{11}, \mathbf{R}_{2}\}; \{\mathbf{R}_{3}, \mathbf{R}_{1}, \mathbf{R}_{9}\}; \{\mathbf{R}_{10}, \mathbf{R}_{6}\}$	[0.140]
11	$\{\mathbf{R}_{8}, \mathbf{R}_{13}, \mathbf{R}_{4}, \mathbf{R}_{12}, \mathbf{R}_{14}, \mathbf{R}_{5}, \mathbf{R}_{7}, \mathbf{R}_{3}, \mathbf{R}_{1}, \mathbf{R}_{9}\}; \{\mathbf{R}_{11}, \mathbf{R}_{2}\}; \{\mathbf{R}_{10}, \mathbf{R}_{6}\}$	[0.207]
12	$\{\mathbf{R_{11}}, \mathbf{R_2}, \mathbf{R_{10}}, \mathbf{R_6}\}; \{\mathbf{R_8}, \mathbf{R_{13}}, \mathbf{R_4}, \mathbf{R_{12}}, \mathbf{R_{14}}, \mathbf{R_5}, \mathbf{R_7}, \mathbf{R_3}, \mathbf{R_1}, \mathbf{R_9}\}$	[0.209]
13	$\{R_{11}, R_2, R_{10}, R_6, R_8, R_{13}, R_4, R_{12}, R_{14}, R_5, R_7, R_3, R_1, R_9\}$	[0.435]

Note: Values in the brackets represent merging distance

It is easy to establish the metric properties of  $d_w(R_pR_j)$ . The intuitive justification of  $d_w(R_pR_j)$  and its being a metric enable  $d_w$ -based clustering of ARs.

#### 4. $d_w$ -BASED CLUSTERING OF ARs

Table 1 represents an artificial transaction database consisting of 100 transactions; the complete item-set being {*Bread*, *Butter*, *Jam*, *Milk*, *Chocolate*, *Biscuit*, *Pen*, *Pencil*, *Eraser*}. It contains fifteen unique market-baskets. Support and confidence having respective thresholds of 0.1 and 0.5 yielded fourteen ARs listed in Table 2.

 $R_{6}$  and  $R_{7}$  have two common items namely, *Chocolate* and *Biscuit*.  $R_{7}$  has a higher w-value. Support of  $R_{7}$  (0.11) is much lower than that of  $R_{6}$ (0.24). Hence  $R_{7}$  is not able to account for the presence of {*Chocolate*,*Biscuit*} as much as  $R_{6}$ . Secondly, presence of *Milk* in  $R_{7}$ further increases its *weakness*-value because  $R_{7}$  is able to explain the presence of *Milk* in only 11 of the 50 transactions (22.0%) that contain *Milk.* However, a high support value does not guarantee a low *weakness*-value.  $R_3$ 's *weakness*-value (Support=0.30, w=0.334146) demonstrates this.  $R_3$ 's support though high is not sufficient to cover the presence of *Bread* and *Milk*.

Table 3 lists the clusters obtained through the average-linkage method [4]. Despite the difference (0.017523) in the *weakness*-values between  $R_{14}$  and  $R_5$  being greater than the difference (0.010614) between  $R_{10}$  and  $R_6$ , the former pair merges earlier.  $R_{14}$  and  $R_5$  being *weaker* rules leads to lesser inter-rule distance as compared to  $R_{10}$  and  $R_6$ .

A rule and its sub-rules being in different clusters may be due to the difference in support between a rule and its sub-rules. If the support values of a rule's items have wide variation, then different sub-rules may explain their constituents' presence to different extents. This difference in their *weakness*-values may place them in different clusters. Cluster configuration after Step 9 results in clusters  $C_{w1}$ :  $\{R_{1a}, R_5, R_7\}$  and  $C_{w2}$ :  $\{R_{1a}, R_6\}$  whose elements have an average *w*-values of 0.608383 and 0.141671 respectively.  $R_7$  is a member of high-*weakness*  $C_{w2}$  respectively. Support values of clusters  $C_{w1}$  and  $low-weakness C_{w2}$  respectively. Support values of constituents *Milk* (0.50), *Chocolate* (0.33) and *Biscuit* (0.24) also show some variation. Thus, low-support coupled with high variation in the support values of its constituents might result in a *weak* rule.

Surprisingly, rules describing *Milk* (the most frequent item) belong to high-*weakness* clusters. None of the rules that contain *Milk* covers its presence to a substantial extent. High support of *Milk* also increases the *weakness* of low-support rules that contain it. Thus, a frequently occurring item may be present in many high-*weakness* rules if the item is purchased in many non-overlapping low-support market-baskets.

Another observation is with respect to rules in clusters that have relatively lower average *weakness*-values. Low-*weakness* clusters may not contain high-support rules. Consider  $C_{w2}$ : { $R_{10}$ ,  $R_6$ }. Note that support of  $R_{10}$  (0.23) is quite close to support of its items *Pencil* (0.28) and *Eraser* (0.26). High explanatory power of such a rule is derived from its support value being close to the support values of its constituent items.

# 5. COMPARATIVE ANALYSIS AND DISCUSSION

Sahar [7] defines  $d_{sc}$ -distance on the basis of difference in rule's itemsets and overlap in the set of transactions that each rule covers.  $d_{sc}$  considers itemsets in antecedent/consequent in their entirety while  $d_w$  considers each item of a rule separately. Table 4 displays  $d_{sc}$ -based cluster configurations.

 $R_g$  is a sub-rule of  $R_g$  both having support 0.13. Their antecedents match completely. Hence contribution due to antecedent dissimilarity towards  $d_{sc}(R_g, R_g)$  is 0. Also,  $R_g$ 's consequent ({*Pencil*}) is a subset  $R_g$ 's consequent ({*Pencil*, *Eraser*}).  $R_g$  covers all transactions covered by  $R_g$  thus increas-

Table 4. d<sub>sc</sub> -based clustering

Step No	Clusters	
1	$\{\mathbf{R}_{9},\mathbf{R}_{8}\}$	[0.429]
2	$\{\mathbf{R}_{12}, \mathbf{R}_{2}\}; \{\mathbf{R}_{9}, \mathbf{R}_{8}\}$	[0.437]
3	$\{\mathbf{R}_{5},\mathbf{R}_{1}\};\{\mathbf{R}_{12},\mathbf{R}_{2}\};\{\mathbf{R}_{9},\mathbf{R}_{8}\}$	[0.442]
4	$\{R_{11}, R_9, R_8\}; \{R_5, R_1\}; \{R_2, R_{12}\}$	[1.098]
5	$\{\mathbf{R}_{4}, \mathbf{R}_{5}, \mathbf{R}_{1}\}; \{\mathbf{R}_{11}, \mathbf{R}_{9}, \mathbf{R}_{8}\}; \{\mathbf{R}_{2}, \mathbf{R}_{12}\}$	[1.892]
6	$\{\mathbf{R}_{13}, \mathbf{R}_{12}, \mathbf{R}_{2}\}; \{\mathbf{R}_{4}, \mathbf{R}_{5}, \mathbf{R}_{1}\}; \{\mathbf{R}_{11}, \mathbf{R}_{9}, \mathbf{R}_{8}\}$	[1.958]
7	$\{\mathbf{R_{10}}, \mathbf{R_{11}}, \mathbf{R_9}, \mathbf{R_8}\}; \{\mathbf{R_{13}}, \mathbf{R_{12}}, \mathbf{R_2}\}; \{\mathbf{R_4}, \mathbf{R_5}, \mathbf{R_1}\}$	[2.244]
8	$\{ {\bm{R_{14}}}, {\bm{R_6}} \}; \{ R_{10}, R_{11}, R_9, R_8 \}; \{ R_{13}, R_{12}, R_2 \}; \{ R_4, R_5, R_1 \}$	[2.313]
9	$\{ \textbf{R_{13}}, \textbf{R_{12}}, \textbf{R_{3}}, \textbf{R_{2}} \}; \{ R_{14}, R_{6} \}; \{ R_{10}, R_{11}, R_{9}, R_{8} \}; \{ R_{4}, R_{5}, R_{1} \}$	[2.734]
10	$\{\mathbf{R_{13}}, \mathbf{R_{12}}, \mathbf{R_3}, \mathbf{R_2}, \mathbf{R_4}, \mathbf{R_5}, \mathbf{R_1}\}; \{\mathbf{R_{14}}, \mathbf{R_6}\}; \{\mathbf{R_{10}}, \mathbf{R_{11}}, \mathbf{R_9}, \mathbf{R_8}\}$	[2.773]
11	$\{\mathbf{R_{7,}R_{14,}R_{6}}\};\{R_{13},R_{12},R_{3},R_{2},R_{4},R_{5},R_{1}\};\{R_{10},R_{11},R_{9},R_{8}\}$	[2.875]
12	$\{\textbf{R_{7},R_{14},R_{6},R_{13},R_{12},R_{3},R_{2},R_{4},R_{5},R_{1}}\},\{\textbf{R_{10},R_{11},R_{9},R_{8}}\}$	[3.980]
13	$\{R_{7},\!R_{14},\!R_{6},\!R_{13},\!R_{12},\!R_{3},\!R_{2},\!R_{4},\!R_{5},\!R_{1},\!R_{10},\!R_{11},\!R_{9},\!R_{8}\}$	[4.437]

Note: Values in the brackets represent merging distance

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ing their similarity. Hence their low  $d_{sc}$ -value (0.429167). Hence  $R_s$  and  $R_q$  merge at Step 1.

 $d_{sc}$ -based clustering is useful in bringing together rules originating from the same portion of a database [7]. Here each cluster consists of rules whose items are members of the same or close domains. However, a rule and its sub-rules may vary a great deal on parameters like explanatory power, etc. Hence, a user may have to examine different clusters to find rules having the same specificity/generality.

Our scheme namely, groups rules having 'similar' values of *weakness* (similar explanatory power) irrespective of their domain. Characteristics like average-*weakness* may be used to define low-*weakness* clusters leading to appropriate clusters for further examination. Rules in other clusters need not be examined thus mitigating the rule immensity problem to some extent.

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