

## Chapter 18

# Structural Intervention and External Control for Markovian Regulatory Network Models

**Xiaoning Qian**  
Texas A&M, USA

**Ranadip Pal**  
Texas Tech University, USA

### ABSTRACT

*In order to derive system-based methods to control dynamic behavior of biological systems of interest for future gene-based intervention therapeutics, two basic categories of intervention strategies have been studied based on the Markov chain theory and Markov decision processes: Structural intervention by function perturbation and external control based on state perturbation. The chapter reviews the existing network analysis and control methods in these two categories and discusses their extensions for more robust and clinically relevant intervention strategies considering collateral damages from intervention.*

### 1. INTRODUCTION

Mathematical modeling and dynamic analysis of gene regulatory networks enable mathematical avenues to study potential systems therapeutics to intervene regulatory networks so that the modeled system dynamics can be altered for desired systems behavior, which is one of the utmost important goals of systems biology from mathematical modeling of biological networks. Network intervention till today has been mostly investigated in the context of probabilistic Boolean networks (PBNs) (Shmulevich & Dougherty, 2007; Shmulevich & Dougherty, 2010; Dougherty, Pal, Qian, Bittner, & Datta, 2010). Two basic categories of intervention strategies have been studied based on the Markov chain theory and Markov decision processes: Structural intervention and external control based on state perturbation.

DOI: 10.4018/978-1-5225-8903-7.ch018

*Structural intervention* or function perturbation involves changing regulatory relationships or wiring among genes in networks (Shmulevich, Dougherty, & Zhang, 2002a; Xiao & Dougherty, 2007; Qian & Dougherty, 2008). The wiring changes cause the changes in the rule-based structure in PBNs and hence state transition of the underlying Markov chains, which further lead to the alteration in long-run network behavior characterized by their steady-state distributions. Given a class of potential structural changes ( $\mathbf{u}_s$ ) in mathematical network models that simulate practical therapeutic strategies by the use of drugs to act on gene products for pathway blockage, for example using small interfering RNAs (siRNAs), the mathematical problem is to derive the structural intervention resulting in an optimal alteration of the steady-state distribution. In order to characterize the dynamic changes caused by structural perturbations and derive effective intervention strategies, we need to mathematically address two critical issues: (1) Efficient characterization of the effects caused by perturbation and (2) search for the optimal perturbation(s) that provides the most desirable steady-state distribution after intervention. We have recently adopted the classical Markov chain perturbation theory to address these problems.

*External control* by state perturbation is generally based on flipping the state of a control gene, hence the concentration of either its corresponding mRNA expression or protein product will be knocked down or over expressed, for beneficial network dynamical change. Corresponding gene expression changes are forced by external perturbations to modulate the dynamics. This type of network intervention models feasible medical treatments for potential therapeutics such as gene knockdown or chemotherapy. Typically, optimal external control is derived in the framework of Markov decision process (Shmulevich, Dougherty, & Zhang, 2002b; Datta, Choudhary, Bittner, & Dougherty, 2003; Bertsekas, 2005; Pal, Datta, & Dougherty, 2006; Datta, Pal, Choudhary, & Dougherty, 2007) for both finite-horizon and infinite-horizon control policies, in which the control action is based on an objective function that rewards beneficial gene activity. Mathematically, we are interested in deriving a control policy  $u_g$  for a given control gene  $g$  or a set of control genes when necessary. At a time point  $t$  if the network state is at  $x$ , the expression state for  $g$  is flipped if  $u_g(x) = 1$ , denoting the control is on. Otherwise when  $u_g(x) = 0$ , the state of the control gene  $g$  remains unchanged. To achieve beneficial network behavior, we minimize the average cost function reflecting the undesirability of the gene activities by deriving the optimal control policy  $u_g$ . For the infinite-horizon problem, stationary control policies can be solved by dynamic programming with networks of reasonable size (Pal *et al.*, 2006; Datta *et al.*, 2007). But for large networks, the optimal solution is often computationally prohibitive. Hence, greedy algorithms are necessary to alter the steady-state network behavior to lessen the likelihood of being in undesirable states, for instance, metastatic states in cancer.

In Figure 1, we schematically illustrate these two types of intervention strategies. We will start with a brief review on PBNs for modeling gene regulatory networks in Section 2. Both methods for structural intervention (Section 3) and external control (Section 4) will be discussed, followed by further extensions considering both potential side effects (Section 5) and robustness of intervention strategies (Section 6) for practical usage.

## 2. BACKGROUNDS

One way to model dynamic behavior of gene regulatory networks is to consider the time evolution of gene expression profiles as dependent stochastic processes regulated by each other. The dynamics of each individual gene, for example, the  $i$ th gene, involved in a given biological process, can be manifested by

28 more pages are available in the full version of this document, which may be purchased using the "Add to Cart" button on the publisher's webpage:

[www.igi-global.com/chapter/structural-intervention-and-external-control-for-markovian-regulatory-network-models/228634](http://www.igi-global.com/chapter/structural-intervention-and-external-control-for-markovian-regulatory-network-models/228634)

## Related Content

---

### Process Optimization Study of Alternative Fuel Production From Linseed Oil

Karthickeyan V., Balamurugan S., Ashok B., Thiyagarajan S., Mohamed Shameer P. and Dhinesh Balasubramanian (2020). *Recent Technologies for Enhancing Performance and Reducing Emissions in Diesel Engines* (pp. 234-249).

[www.irma-international.org/chapter/process-optimization-study-of-alternative-fuel-production-from-linseed-oil/249066](http://www.irma-international.org/chapter/process-optimization-study-of-alternative-fuel-production-from-linseed-oil/249066)

### Deep Learning and Biomedical Engineering

Suraj Sawant (2019). *Biotechnology: Concepts, Methodologies, Tools, and Applications* (pp. 562-575).

[www.irma-international.org/chapter/deep-learning-and-biomedical-engineering/228639](http://www.irma-international.org/chapter/deep-learning-and-biomedical-engineering/228639)

### Big Data Analysis Techniques for Visualization of Genomics in Medicinal Plants

Hithesh Kumar, Vivek Chandramohan, Smrithy M. Simon, Rahul Yadav and Shashi Kumar (2019). *Biotechnology: Concepts, Methodologies, Tools, and Applications* (pp. 804-837).

[www.irma-international.org/chapter/big-data-analysis-techniques-for-visualization-of-genomics-in-medicinal-plants/228649](http://www.irma-international.org/chapter/big-data-analysis-techniques-for-visualization-of-genomics-in-medicinal-plants/228649)

### Effect of Additives on the Performance and Emission Attributes of Diesel Engines

Shanmuga Sundaram. N. and Sivakumar Muthusamy (2020). *Recent Technologies for Enhancing Performance and Reducing Emissions in Diesel Engines* (pp. 65-84).

[www.irma-international.org/chapter/effect-of-additives-on-the-performance-and-emission-attributes-of-diesel-engines/249058](http://www.irma-international.org/chapter/effect-of-additives-on-the-performance-and-emission-attributes-of-diesel-engines/249058)

### Information Needs of Bioinformatics Researchers

Manlunching (2019). *Biotechnology: Concepts, Methodologies, Tools, and Applications* (pp. 1268-1276).

[www.irma-international.org/chapter/information-needs-of-bioinformatics-researchers/228669](http://www.irma-international.org/chapter/information-needs-of-bioinformatics-researchers/228669)