

Cluster Analysis in Fitting Mixtures of Curves

Tom Burr

Los Alamos National Laboratory, USA

C

INTRODUCTION

One data mining activity is cluster analysis, which consists of segregating study units into relatively homogeneous groups. There are several types of cluster analysis; one type deserving special attention is clustering that arises due to a mixture of curves. A mixture distribution is a combination of two or more distributions. For example, a bimodal distribution could be a mix with 30% of the values generated from one unimodal distribution and 70% of the values generated from a second unimodal distribution.

The special type of mixture we consider here is a mixture of curves in a two-dimensional scatter plot. Imagine a collection of hundreds or thousands of scatter plots, each containing a few hundred points including background noise but also containing from zero to four or five bands of points, each having a curved shape. In one application (Burr et al. 2001), each curved band of points was a potential thunderstorm event (see Figure 1) as observed from a distant satellite and the goal was to cluster the points into groups associated with thunderstorm events. Each curve has its own shape, length, and location, with varying degrees of curve overlap, point density, and noise magnitude. The scatter plots of points from curves having small noise resemble a smooth curve with very little vertical variation from the curve, but there can be a wide range in noise magnitude so that some events have large vertical variation from the center of the band. In this context, each curve is a cluster and the challenge is to use only the observations to estimate how many curves comprise the mixture, plus their shapes and locations. To achieve that goal, the human eye could train a classifier by providing cluster labels to all points in example scatter plots. Each point would either belong to a curved-region or to a catch-all noise category and a specialized cluster analysis would be used to develop an approach for labeling (clustering) the points generated according to the same mechanism in future scatter plots.

BACKGROUND

Two key features that distinguish various types of clustering approaches are the assumed mechanism for how the data is generated and the dimension of the data. The data-generation mechanism includes deterministic and stochastic components and often involves deterministic mean shifts between clusters in high dimensions. But there are other settings for cluster analysis. The particular one discussed here involves identifying thunderstorm events from satellite data as described in the Introduction. From the four examples in Figure 1, note that the data can be described as a mixture of curves where any notion of a cluster mean would be quite different from that in more typical clustering applications. Furthermore, although finding clusters in a two-dimensional scatter plot seems less challenging than in higher-dimensions (the trained human eye is likely to perform as well as any machine-automated method, although the eye would be slower), complications include: overlapping clusters, varying noise magnitude, varying feature and noise and density, varying feature shape, locations, and length, and varying types of noise (scene-wide and event-specific). Any one of these complications would justify treating the fitting of curve mixtures as an important special case of cluster analysis.

Although as in pattern recognition, the methods discussed below require training scatter plots with points labeled according to their cluster memberships, we regard this as cluster analysis rather than pattern recognition because all scatter plots have from zero to four or five clusters whose shape, length, location, and extent of overlap with other clusters varies among scatter plots. The training data can be used to both train clustering methods, and then judge their quality. Fitting mixtures of curves is an important special case that has received relatively little attention to date. Fitting mixtures of probability distributions dates to Titterton et al. (1985), and several model-based clustering schemes have been developed (Banfield and

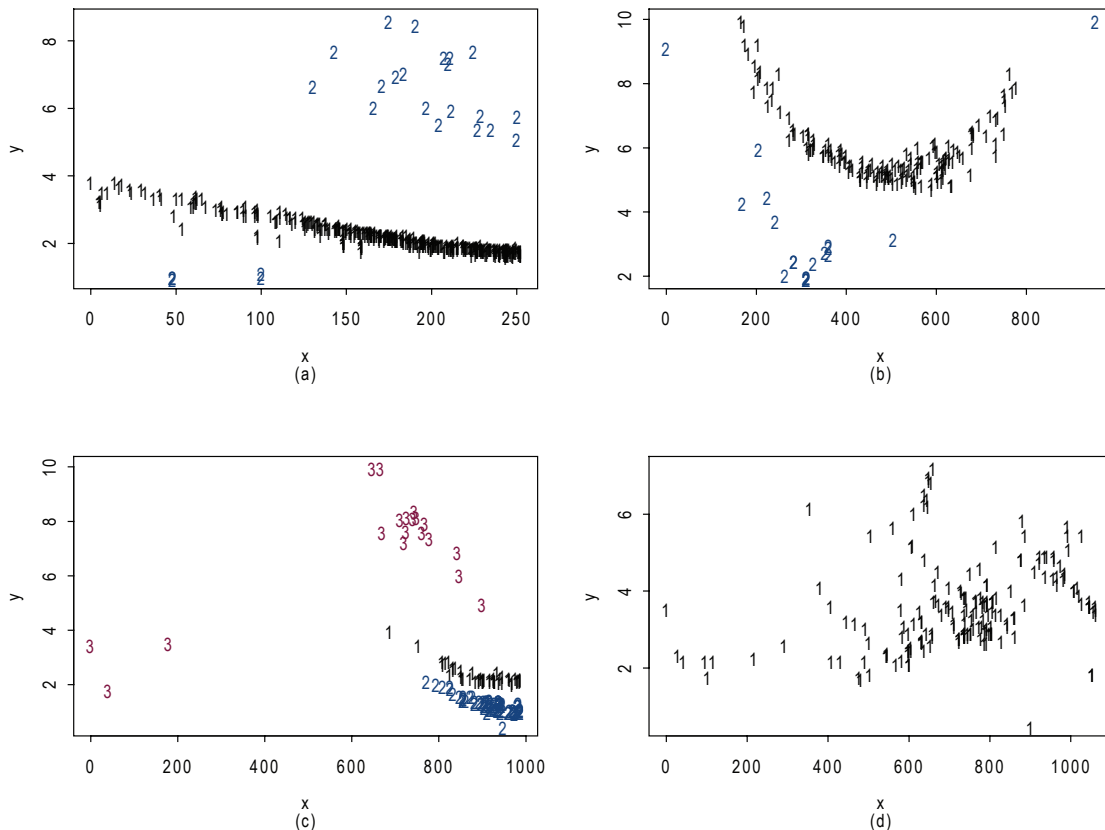
Raftery, 1993, Bensmail et al., 1997 and Dasgupta and Raftery, 1998) along with associated theory (Leroux, 1992). However, these models assume that the mixture is a mixture of probability distributions (often Gaussian, which can be long and thin, ellipsoidal, or more circular) rather than curves. More recently, methods for mixtures of curves have been introduced, including a mixture of principal curves model (Stanford and Raftery, 2000), a mixture of regressions model (Turner, 2000; Gaffney and Smyth 2003, and Hurn, Justel, and Robert, 2003), and mixtures of local regression models (smooth curves obtained using splines or nonparametric kernel smoothers for example)

MAIN THRUST OF THE CHAPTER

We describe four methods have been proposed for fitting mixtures of curves. In method 1 (Burr et al.,

2001), density estimation is used to reject the background noise points such as those labeled as 2 in Figure 1a. For example, each point has a distance to its k th nearest neighbor, which can be used as a local density estimate (Silverman, 1986) to reject noise points. Next, use a distance measure that favors long thin clusters (for example, let the distance between clusters be the minimum distance between a point in the first cluster and a point in the second cluster) together with standard hierarchical clustering to identify at least the central portion of each cluster. Alternatively, model-based clustering favoring long, thin Gaussian shapes (Banfield and Raftery, 1993) or the “fitting straight lines” method in Campbell et al. (1997) are effective for finding the central portion of each cluster. A curve fitted to this central portion can be extrapolated and then used to accept other points as members of the cluster. Because hierarchical clustering cannot accommodate overlapping clusters, this method assumes that the central

Figure 1. Four mixture examples containing (a) one, (b) one, (c) two, and (d) zero thunderstorm events plus background noise. The label “1” is for the first thunderstorm in the scene, “2” for the second, etc., and the highest integer label is reserved for the catch-all “noise” class. Therefore, in (d), because the highest integer is 1, there is no thunderstorm present (the “mixture” is all noise)



4 more pages are available in the full version of this document, which may be purchased using the "Add to Cart" button on the publisher's webpage: www.igi-global.com/chapter/cluster-analysis-fitting-mixtures-curves/10824

Related Content

The Evolution of SDI Geospatial Data Clearinghouses

Caitlin Kelly Maurie (2009). *Encyclopedia of Data Warehousing and Mining, Second Edition* (pp. 802-809).
www.irma-international.org/chapter/evolution-sdi-geospatial-data-clearinghouses/10912

Spectral Methods for Data Clustering

Wenyuan Li (2009). *Encyclopedia of Data Warehousing and Mining, Second Edition* (pp. 1823-1829).
www.irma-international.org/chapter/spectral-methods-data-clustering/11066

Sentiment Analysis of Product Reviews

Cane W.K. Leung (2009). *Encyclopedia of Data Warehousing and Mining, Second Edition* (pp. 1794-1799).
www.irma-international.org/chapter/sentiment-analysis-product-reviews/11061

Positive Unlabelled Learning for Document Classification

Xiao-Li Li (2009). *Encyclopedia of Data Warehousing and Mining, Second Edition* (pp. 1552-1557).
www.irma-international.org/chapter/positive-unlabelled-learning-document-classification/11026

Robust Face Recognition for Data Mining

Brian C. Lovell, Shaokang Chen and Ting Shan (2009). *Encyclopedia of Data Warehousing and Mining, Second Edition* (pp. 1689-1695).
www.irma-international.org/chapter/robust-face-recognition-data-mining/11045